IS-LM Equilibrium

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Objectives

In this section you will learn how to

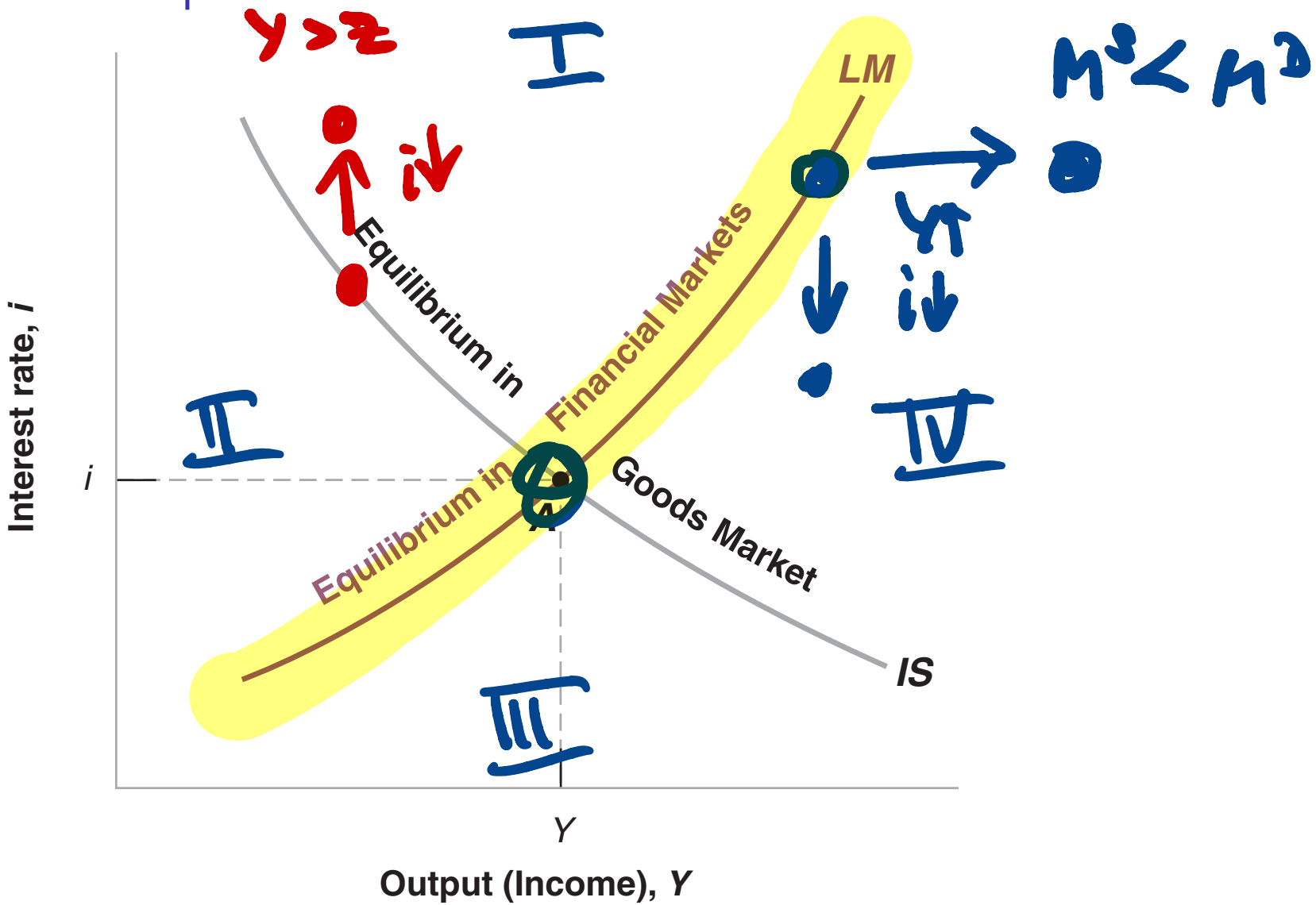
1. put IS and LM together and derive the equilibrium;
2. determine the effects of shocks and policies on equilibrium output and interest rate

Model Summary

- Endogenous objects: Y, i
- Exogenous objects: $\bar{I}, c_0, G, T$
  - also M, which we take as controlled by CB for now
- Equations:
  - IS: $Y = C(Y - T) + I(Y, i) + G$
  - LM: $M/P = YL(i)$

Interactive IS-LM Model

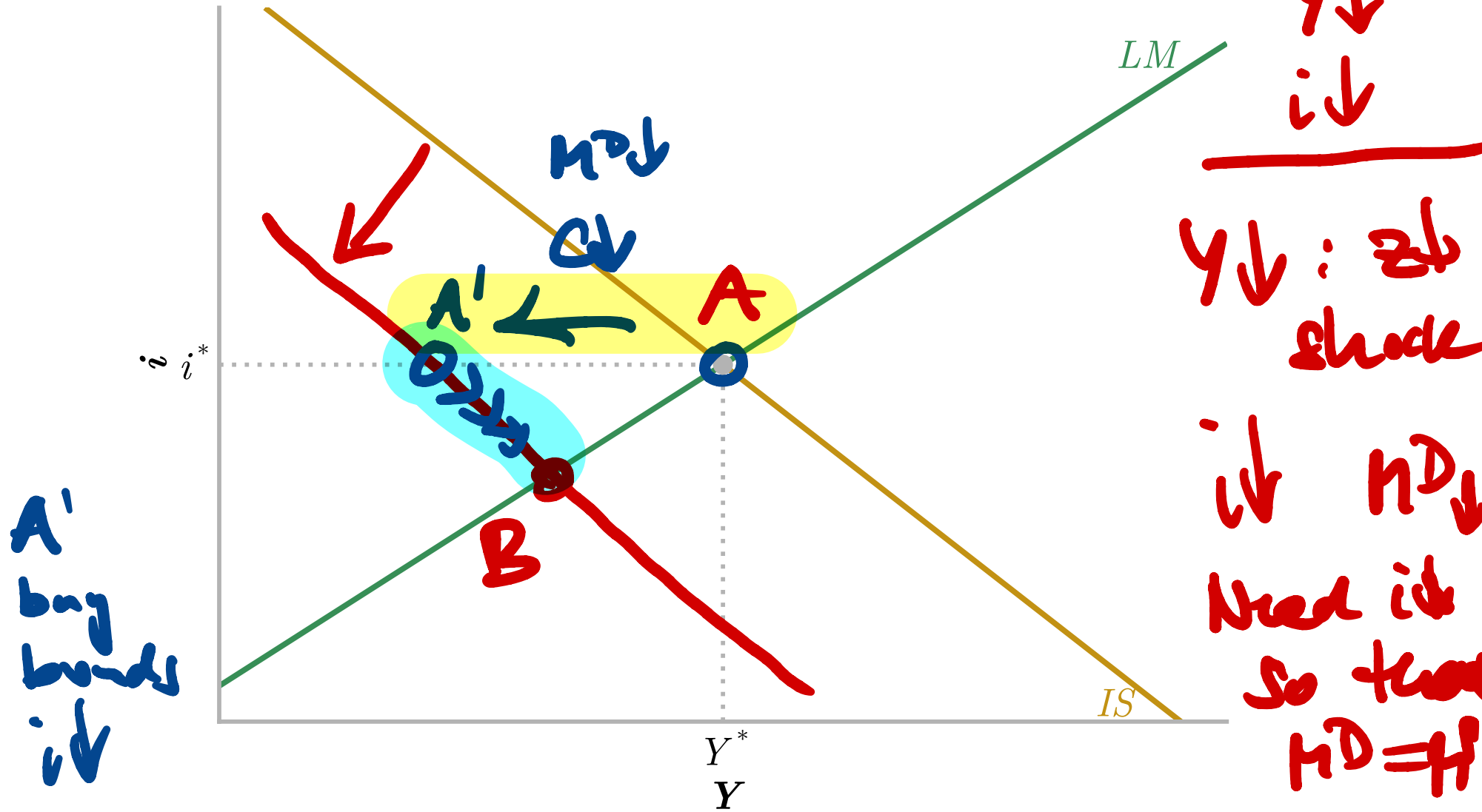
IS-LM Graph



What happens in each market in each quadrant?

2. Applications

2.1 Increasing Taxes



IS: $Y = C(Y-T) + I(Y,i) + G$. LM: $M/P = YL(i)$. The shock: $T \uparrow$

The process...

Taxes and Investment

- A common argument:
  - higher taxes reduce disposable income and saving
  - saving = investment
  - **investment must fall**
- Another common argument:
  - higher taxes reduce the government deficit
  - more money available for investment
  - **investment rises**
- Which argument is right?

private

public

What happens in the model?

Identity: $I = S^P + S^G$

Public saving: $S^G = T - G$

- rises by the change in T
- assuming G is unchanged!

Private saving: $S^P = Y - T - C(Y - T)$

- $(Y - T)\downarrow$
- $MPC < 1 \implies C\downarrow$ by less than $Y - T$
- $S^P \downarrow$

Net change in S is ambiguous.

Increasing Taxes

What is missing in our analysis?

- The **government budget constraint**.

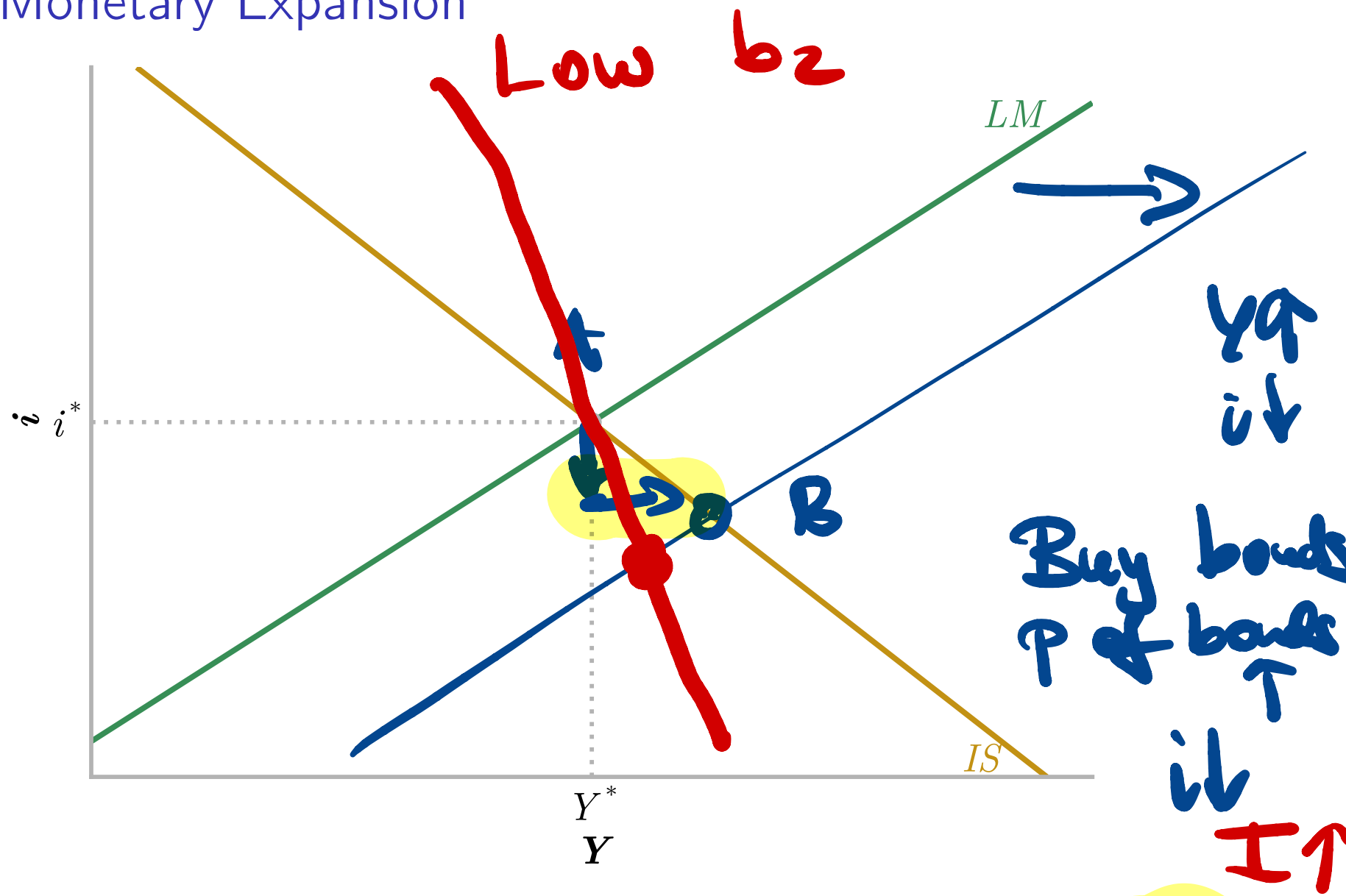
The government cannot raise taxes without changing another policy.

The revenue has to go somewhere.

- Either $G \uparrow$ or public debt $\downarrow$.

A limitation of the IS/LM model.

2.2 Monetary Expansion



IS: $Y = C(Y-T)+I(Y,i)+G$. LM: $M/P = YL(i)$. The shock: $M\uparrow$

Monetary Transmission

The link between monetary and real sector is the interest rate.

$M \uparrow \Longrightarrow i \downarrow \Longrightarrow I \uparrow$

What happens when investment is very interest inelastic?

- $I = \bar{I} + b_1 Y - b_2 i$
- b_2 is small

IS $\quad Y(1-b_1-c_1) = \bar{Z} - b_2 i$

IS steep

2.3 Policy Mix

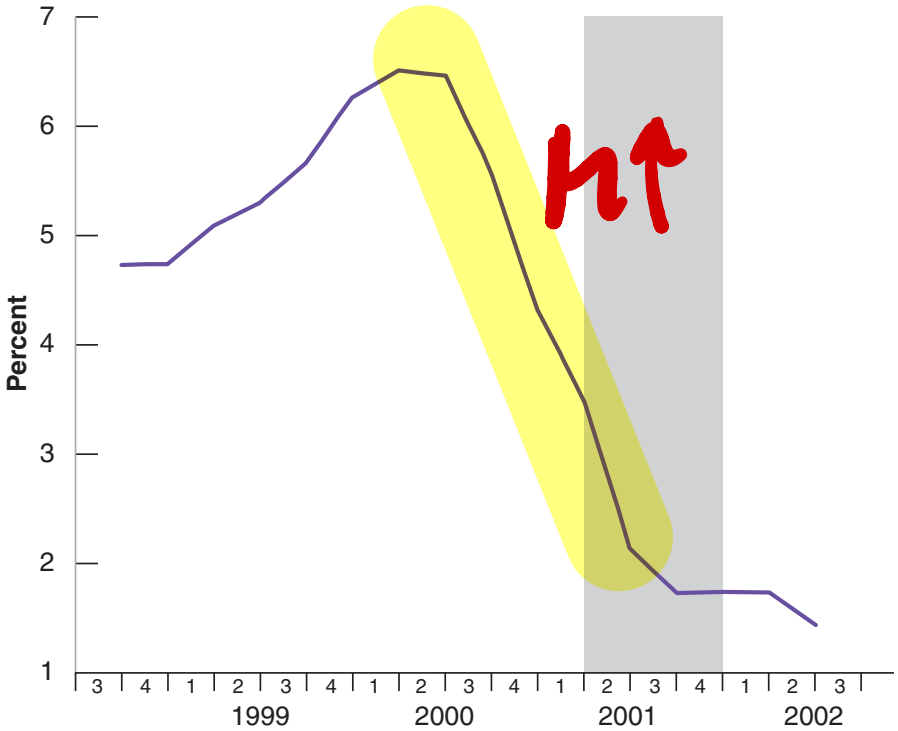
The government can, in principle, move Y and i independently.

- Monetary expansion: $Y \uparrow, i \downarrow$
- Fiscal expansion: $Y \uparrow, i \uparrow$
- Combination: $Y \uparrow, i$ unchanged

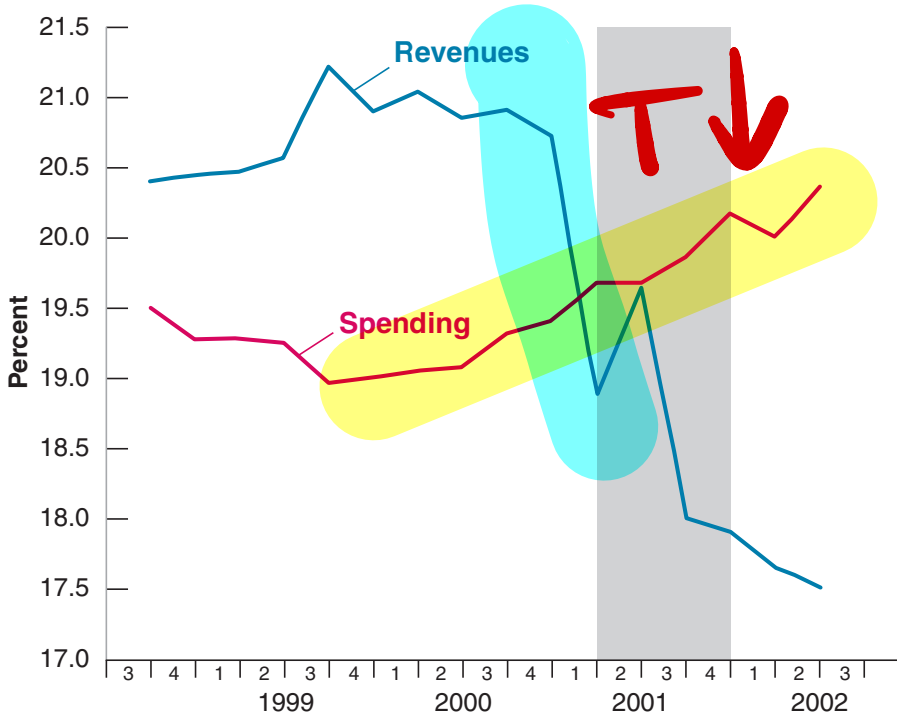
In a typical recession, monetary and fiscal policies expand.

Example: 2001 Recession

The shock: bursting of the tech bubble $\Longrightarrow I \downarrow$



Federal funds rate

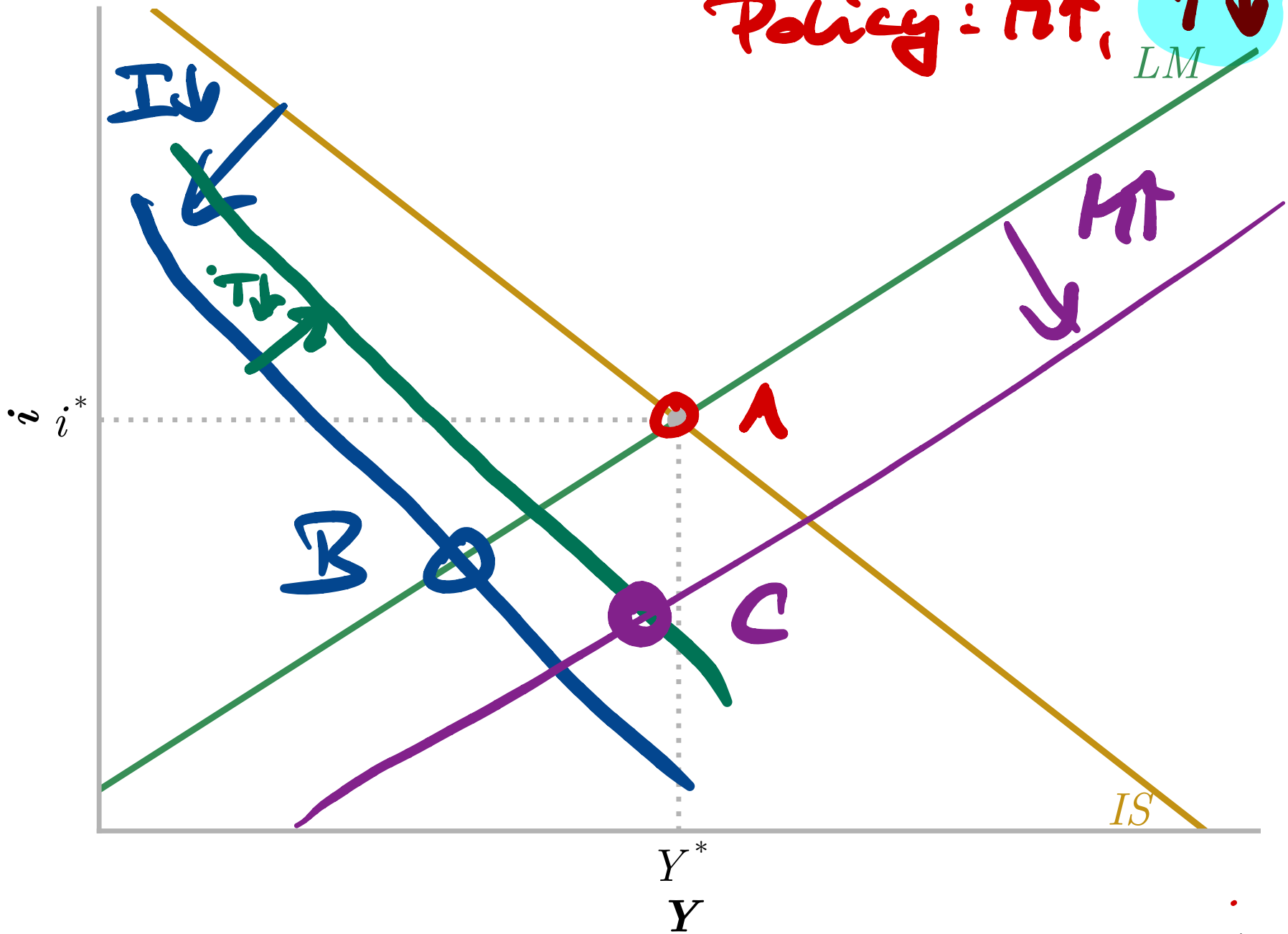


Government spending / revenue

Note that spending moves very slowly.

Revenues drop rapidly (automatic stabilizer).

Analysis of the 2001 Recession

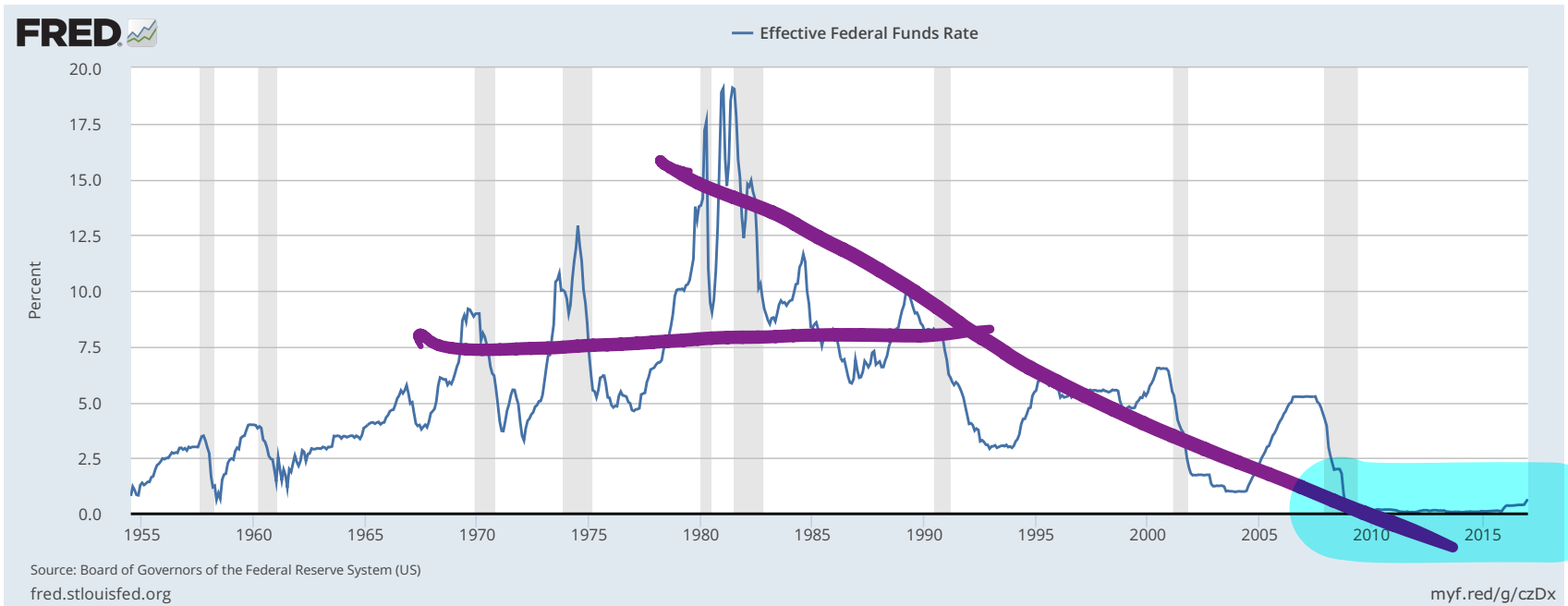


3. Liquidity Traps

Liquidity Traps

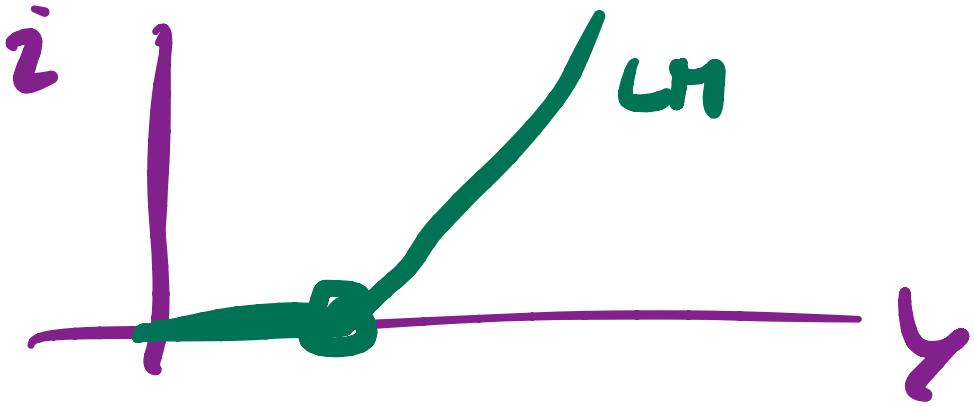
Real interest rates have been near zero for some time.

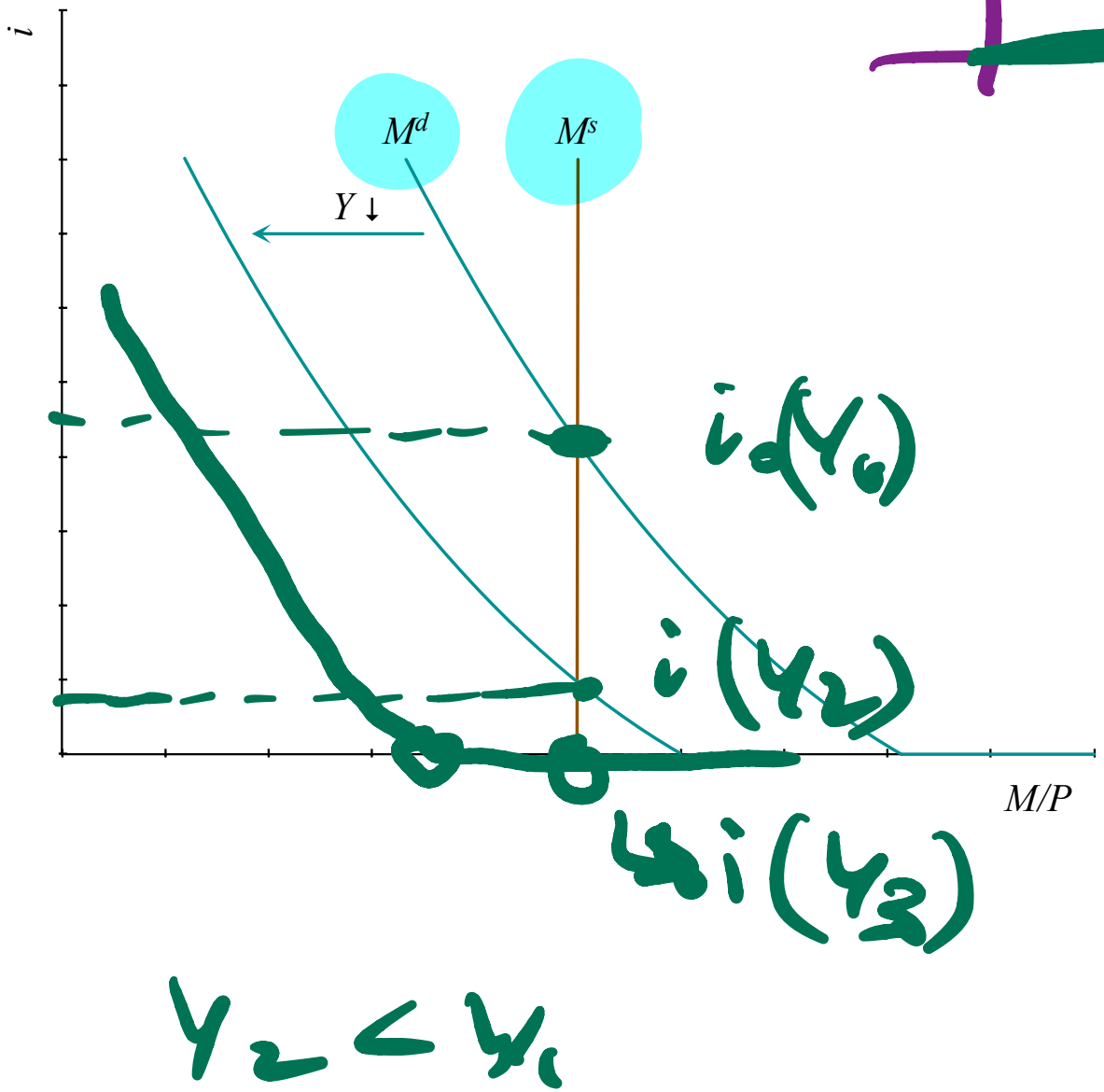
What does this imply for monetary policy?



Source: Fred

Liquidity Trap

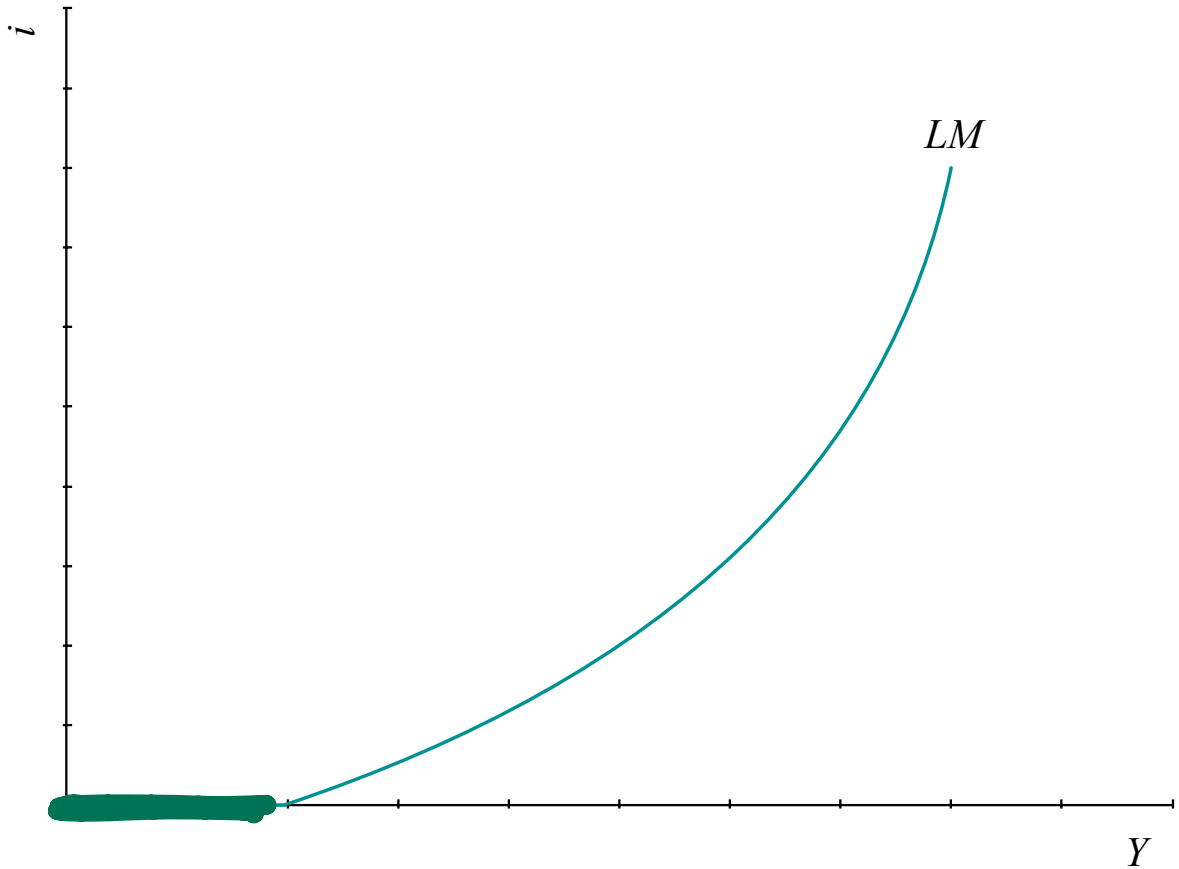




The LM curve turns flat

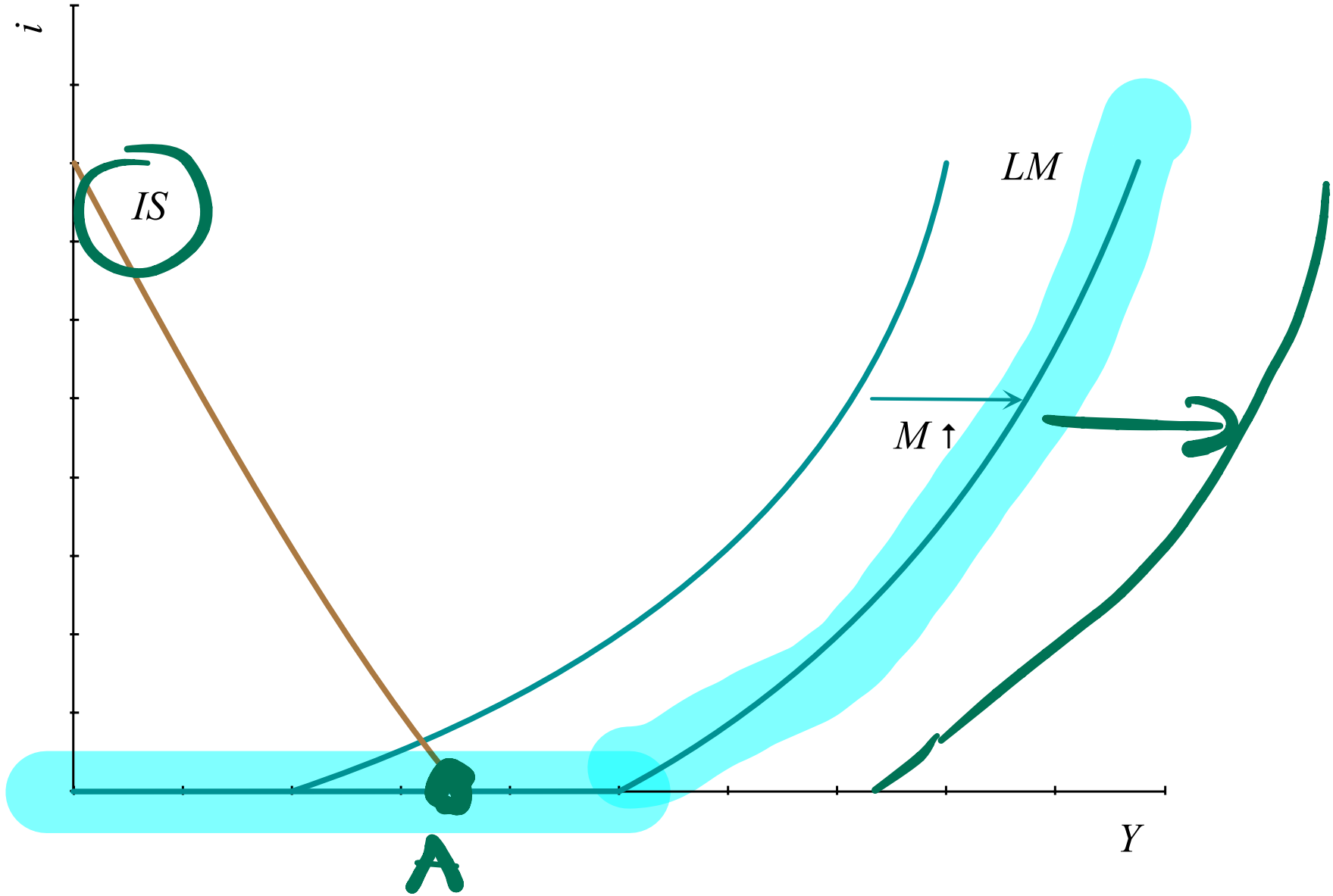
- The LM curve is derived by varying Y and tracing out $i, M/P$ points that clear the money market.
- For low Y the interest rate hits 0 and the LM curve becomes flat.

Liquidity Trap



The LM curve is flat at 0 interest rates.

Liquidity Trap: Monetary Policy



Monetary policy becomes ineffective

Policy options in a liquidity trap

If the interest rate is zero, what can the Fed do?

"QE" Buy bonds w/ $i > 0$

Promise low future i

"Forward guidance"

Promise high inflation

Higher inflation

Low real interest rate

I, C depend on real, not nominal interest

$r = i - \pi$ π inflation

Example

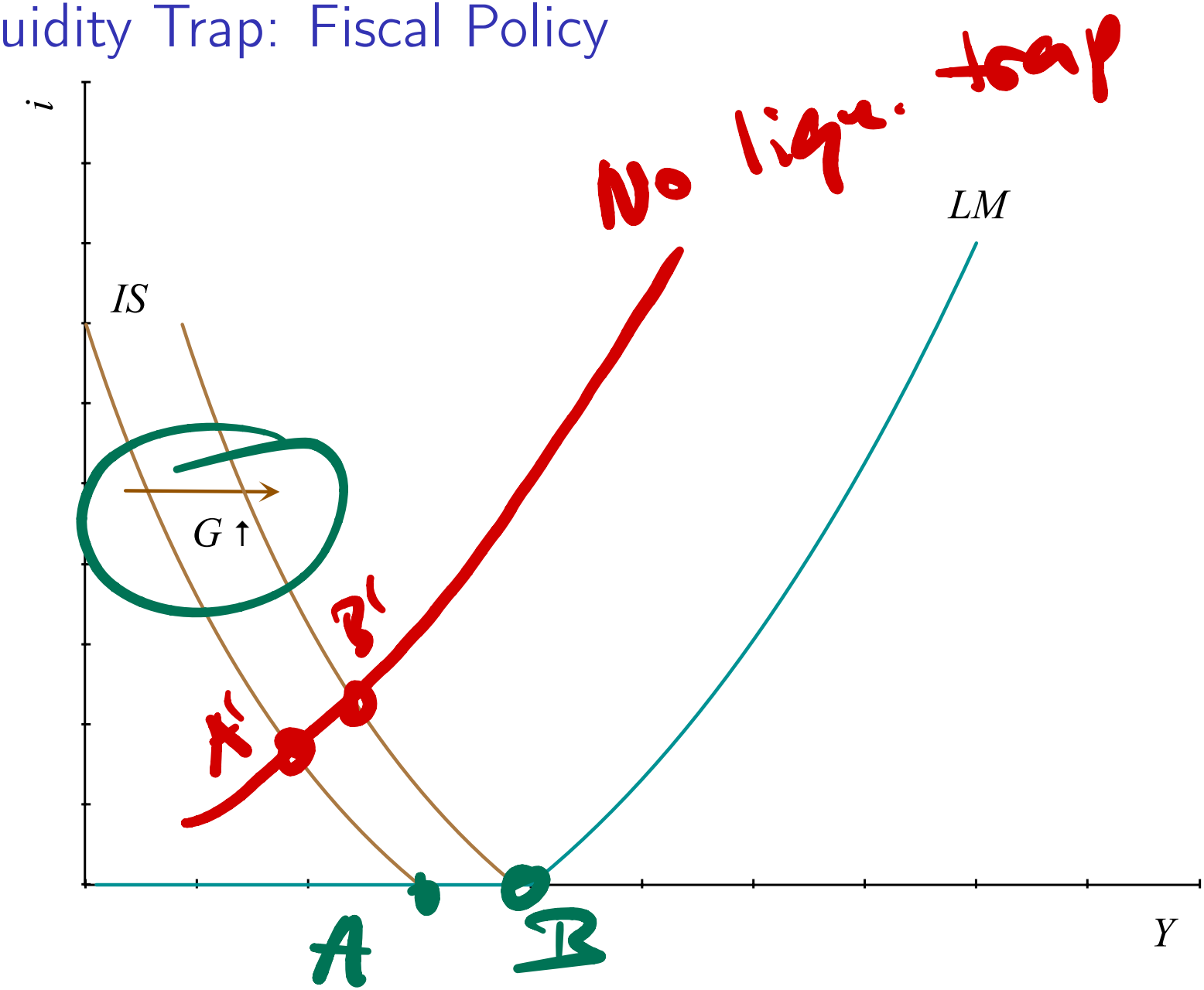
$i = 5\%$

$\pi = 3\%$

$\Big\}\ r = 2\%$

r : relative price of goods over time

Liquidity Trap: Fiscal Policy



Fiscal policy becomes highly effective

4. How Effective are Tax Cuts?

How Effective are Tax Cuts?

Does cutting taxes have a big impact on demand?

How does the answer depend on the MPC?

- MPC = marginal propensity to consume

The answer depends on

- how big is the stimulus (change in demand)?
- how big is amplification?

Stimulus from tax cuts

IS: $Y(1-b_1-c_1) = \bar{Z} + -b_2 i$

with $\bar{Z} = C_0 + I_0 + G - c_1 T$

Stimulus = $c_1 \times \Delta T$ $= \Delta \bar{Z}$

- high $MPC \implies$ large stimulus (intuitive)

How much does IS shift right?

- $\Delta Y \times (1-b_1-c_1) = -c_1 \times \Delta T$ (holding i fixed) $= \Delta \bar{Z}$
- Right shift: $\Delta Y = -\frac{c_1}{1-b_1-c_1} \Delta T$
- High $MPC \implies$ large right shift.

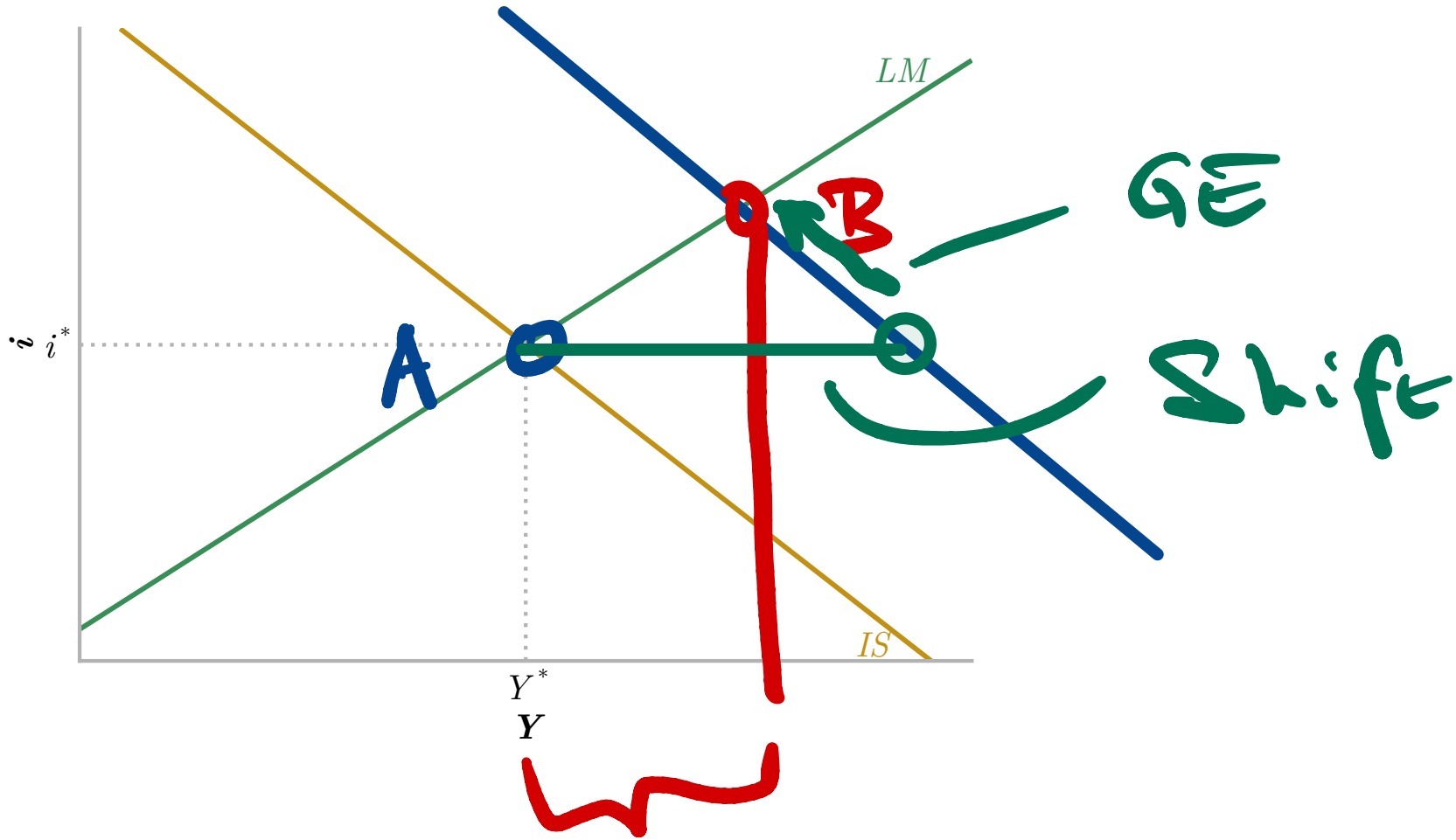
$\Delta Y = -\Delta T \times \frac{c_1}{1-b_1-c_1}$

Shift

Amplification

For a given shift of IS, how much does equilibrium Y rise?

The answer depends on the slope of IS (and LM)



Slope of IS

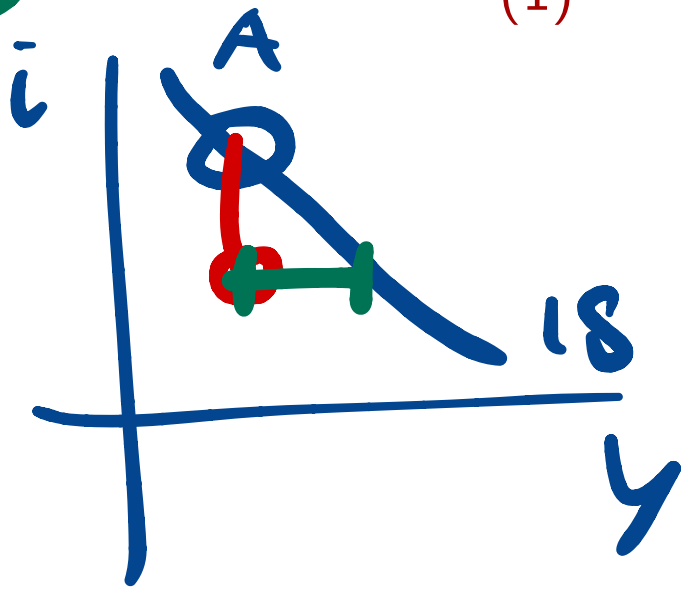
Solve for the interest rate:

$$i = \frac{\bar{Z} - c_1 T - (1 - b_1 - c_1) Y}{b_2} \tag{1}$$

Slope of IS: $-(1 - b_1 - c_1)/b_2$

High MPC c_1 implies

- flat IS
- small change in Y for given shift in IS



Intuition?

Large multiplier

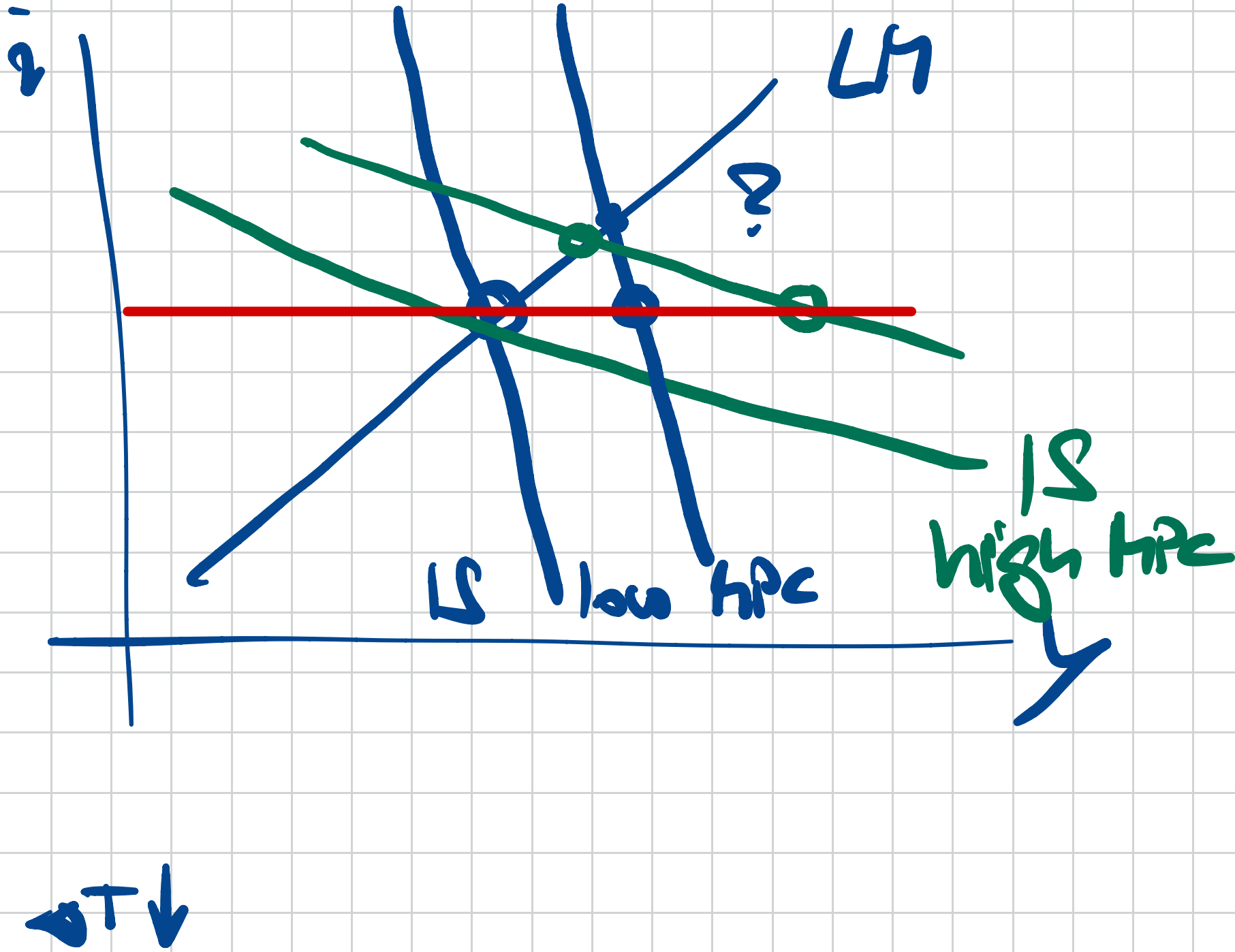
How big is the change in Y?

High MPC means

- big right shift of IS
- lots of crowding out (movement along IS)

Is the answer ambiguous?

- the question being: does a high MPC make tax cuts more or less effective?


i
LM
?
IS
high MPC
IS
low MPC
Y
↓T↓

Second attempt

Let's look at the **vertical shift** of IS:

$$i = \frac{\bar{Z} - (1 - b_1 - c_1)\,Y}{b_2} \tag{2}$$

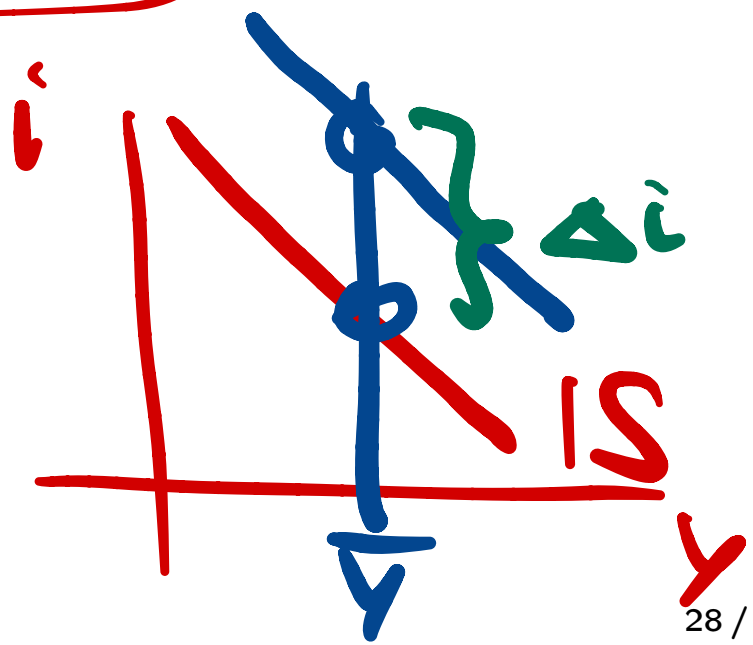
Holding Y constant, the vertical shift is:

$$\Delta i = -\frac{c_1}{b_2} \times \Delta T \tag{3}$$

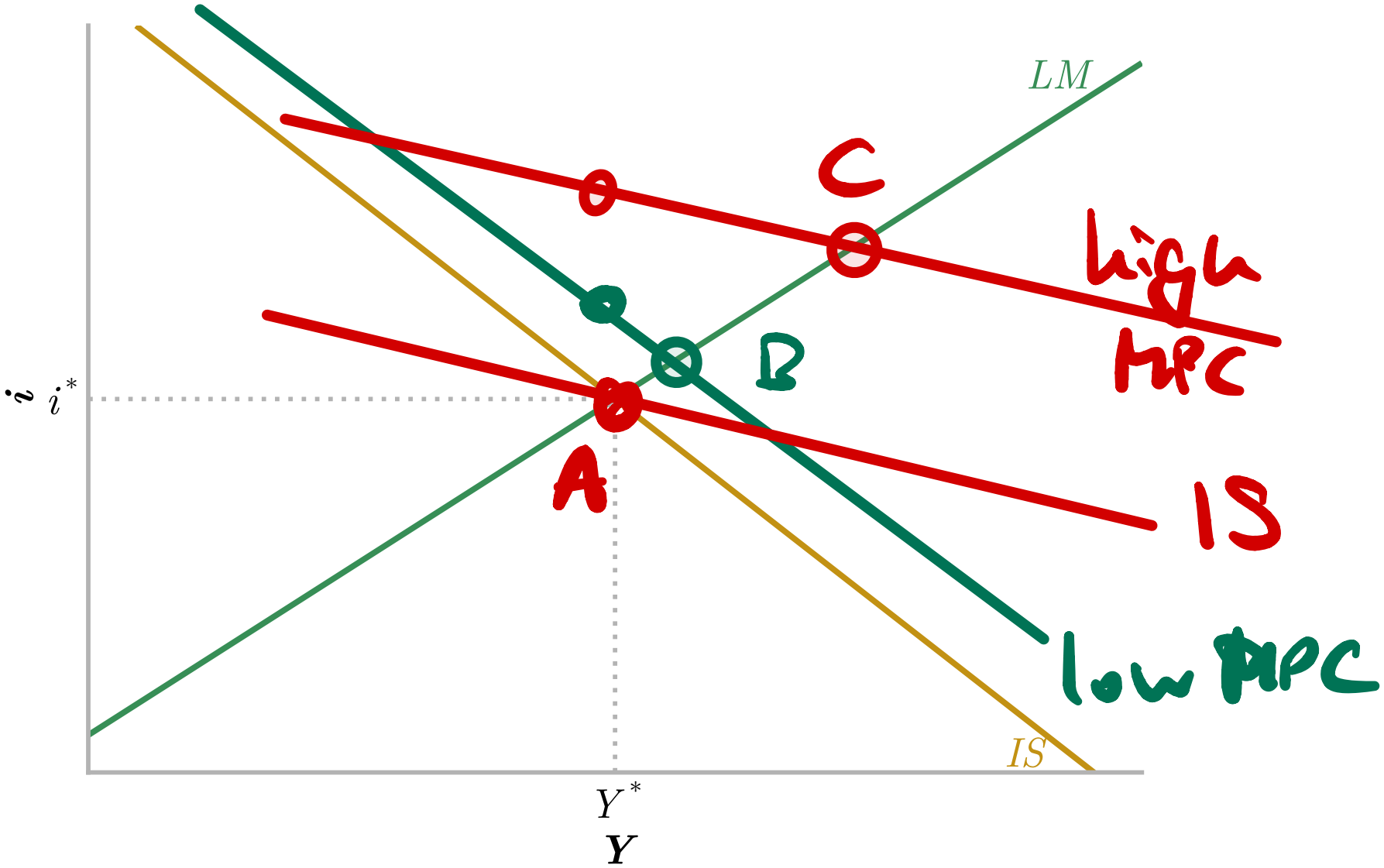
High MPC implies:

- large vertical shift
- ~~flat IS~~

Now what is the total effect on Y?

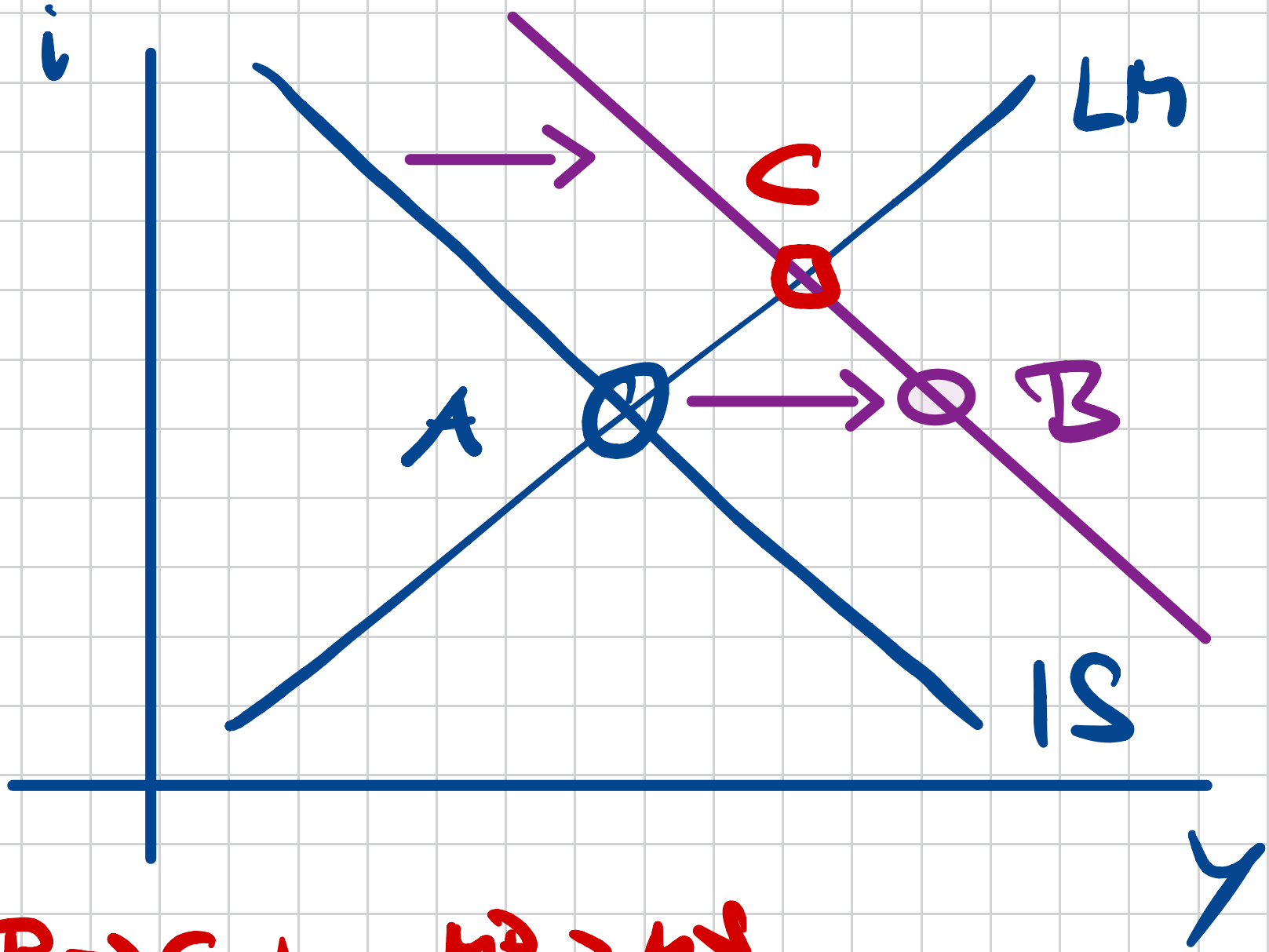


How effective are tax cuts?



High MPC A→C

Low MPC A→B



B → C : $M^D > M^S$

Sell bonds → i↑ → I↓

MPC vs Elasticity

$$C = C_0 + C_1 Y$$

$$MPC \Rightarrow \frac{dC}{dY} = C_1$$

Elasticity of C w.r.to Y

pct change in C for each pct change in Y

Why Elasticities

$$I = \bar{I} + b_1 Y - b_2 i$$

How responsive is I w.r.t to i ?

4.1 How Large is the MPC?

The effectiveness of tax cuts depends critically on the MPC.

How big is the MPC in the data?

> *Empirical estimates of the aggregate marginal propensity to consume (MPC) in the U.S. range from 0.05 to 0.9 depending on the event and sample of the study.*
>
> – *Background: Marginal Propensities to Consume in the 2021 Economy —{} Penn Wharton Budget Model*

That's a pretty wide range!

Why so wide?

How Large is the MPC?

Key point

There is no one MPC.
Each person has their own MPC.
Each stimulus / shock has its own MPC.

A simple model of consumption / saving helps to understand this.

A Simple Model

Assumptions:

- Households like smooth consumption
- They can borrow and lend freely

Budget constraint:

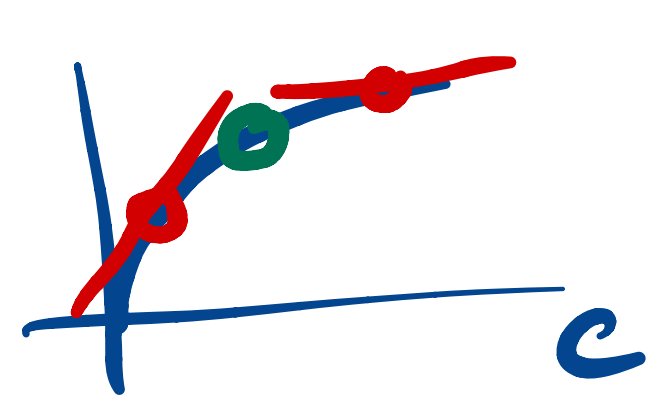
$$\textit{present value of consumption} = \textit{present value of income} + \textit{initial wealth}$$

Why?

- We derive this later for the government
- The same logic applies to any household who can borrow and save

If you want to see the details in a more general model, see the slides from previous years.

A Simple Model



Households live for T periods.

Exogenous income stream y_t

Consumption prices: p_t (in units of account)

Preferences:

$$\sum_{t=1}^{T} U(c_t) \tag{4}$$

Key assumption: diminishing marginal utility of c

- $U'(c) > 0$ but $U''(c) < 0$ (graph)
- this is what causes household to want smooth consumption

A Simple Model

Interest rate = 0

Budget constraint:

$$Y = \sum_{t=1}^{T} y_t = \sum_{t=1}^{T} p_t c_t \tag{5}$$

Solving this problem: Lagrangian

$$\mathscr{L} = \sum_{t=1}^{T} U(c_t) + \lambda \left[Y - \sum_{t=1}^{T} p_t c_t \right] \tag{6}$$

Lagrangian Review

Let's take a simple static problem.

The household values consumption and leisure: $U(c) - v(l)$

subject to the constraint $pc = wl$

Set up the **Lagrangian**

$$\mathscr{L} = \underbrace{U(c) - v(l)}_{\text{objective}} + \lambda \times \underbrace{[wl - pc]}_{\text{constraint}} \tag{7}$$

λ is the **Lagrange multiplier**.

- the value of relaxing the constraint a bit
- in this case: the value of a unit of additional income
- in units of account!

First order (optimality) conditions are

$$\frac{\partial \mathscr{L}}{\partial c} = 0 \implies U'(c) = \lambda p \tag{8}$$

$$\frac{\partial \mathscr{L}}{\partial l} = 0 \implies v'(l) = \lambda w \tag{9}$$

$$\mathcal{L} = u(c) + v(1-e) + \lambda [we - pc]$$

$$v'(1-e) = \lambda w$$

Lagrangian Review

In words:

1. $U'(c) = \lambda p$
   An additional unit of income (relaxing the constraint) c
   can be used to buy $1/p$ units of consumption
   with marginal utility $U'(c)$
2. $v'(l) = \lambda w$
   An additional hour of working costs marginal utility $v'(l)$
   It earns w units of income, each worth λ

A Simple Model

The Lagrangian again:

$$\mathscr{L} = \sum_{t=1}^{T} U(c_t) + \lambda \left[Y - \sum_{t=1}^{T} p_t c_t \right] \tag{10}$$

First-order conditions:

$$U'(c_t) = \lambda p_t \tag{11}$$

In words...

Key implication: if prices are smooth, **households want smooth consumption**

Intuition...

A Simple Model

Simplifying assumption: prices p_t are constant

- this actually means: constant real interest rate
- makes the math simpler without changing main message

Then households want **constant consumption**:

$$U'(c_t) = \lambda \tag{12}$$

- $c_t = \bar{c}$
- more general: smooth consumption, but the implications are the same

Marginal Propensity to Consume

Lifetime (present value) budget constraint:

$$\underbrace{\sum_{t=1}^{T} c_t}_{\text{PV of cons.}} = T\bar{c} = \underbrace{\sum_{t=1}^{T} (y_t - Tax_t)}_{\text{PV of income}} + a_1 \tag{13}$$

Solve for consumption:

$$\bar{c} = \frac{1}{T}\left[\sum_{t=1}^{T} (y_t - Tax_t) + a_1\right] \tag{14}$$

MPC out of one year's income: $\partial \bar{c}/\partial y_t = 1/T$

- age $t = 20$; life-expectancy $T = 85 - 20$: MPC $= 1/65$
- age $t = 50$; life-expectancy $T = 85 - 50$: MPC $= 1/35$

Implications

The MPC out of **current** income should be **small** for most people.

- key, robust intuition ...

But **permanent** tax cuts are very different.

- MPC = ... 1

Expectations of future income matter a lot.

- we come back to that point later.

So one-time tax cuts are hopeless for stimulating the economy?

- who has a high MPC?

Implications

Tax cuts can be effective, but they need to target the right populations.

- tax cuts that benefit the rich are mostly saved
- tax cuts that benefit the poor are mostly consumed

REVIEW: CONSUMPTION

① Households aim for smooth consumption.

Why?

② MPC for one time payment is ... small

Why?

③ Expectations are important

5. The Role of Expectations

The Role of Expectations

Consumption and investment decisions are forward looking.

Future output increases today's spending.

Implications for policy:

1. Expectations become a policy tool.
2. Persistent policies are stronger than temporary ones.

Expectations: Monetary Policy

A monetary expansion now has 2 effects:

1. direct: $i \downarrow \Longrightarrow LM$ shifts right
2. indirect: expectations change

Transitory monetary expansion:

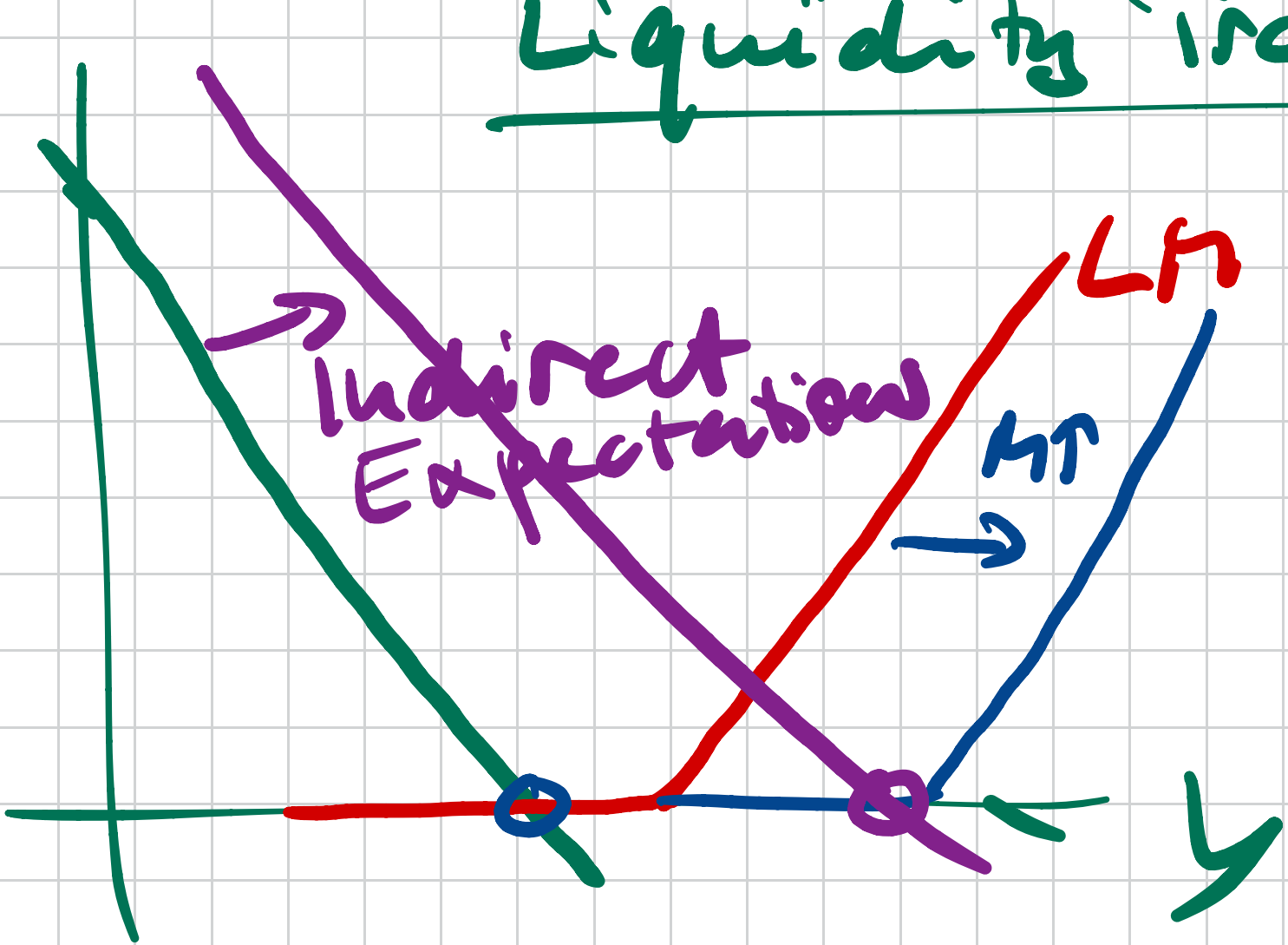
- no change in future Y', i' (primes denote future)
- small policy effect

Persistent monetary expansion:

- expect LM to stay shifted
- $Y' \uparrow$ and $i' \downarrow$
- IS shifts right as well

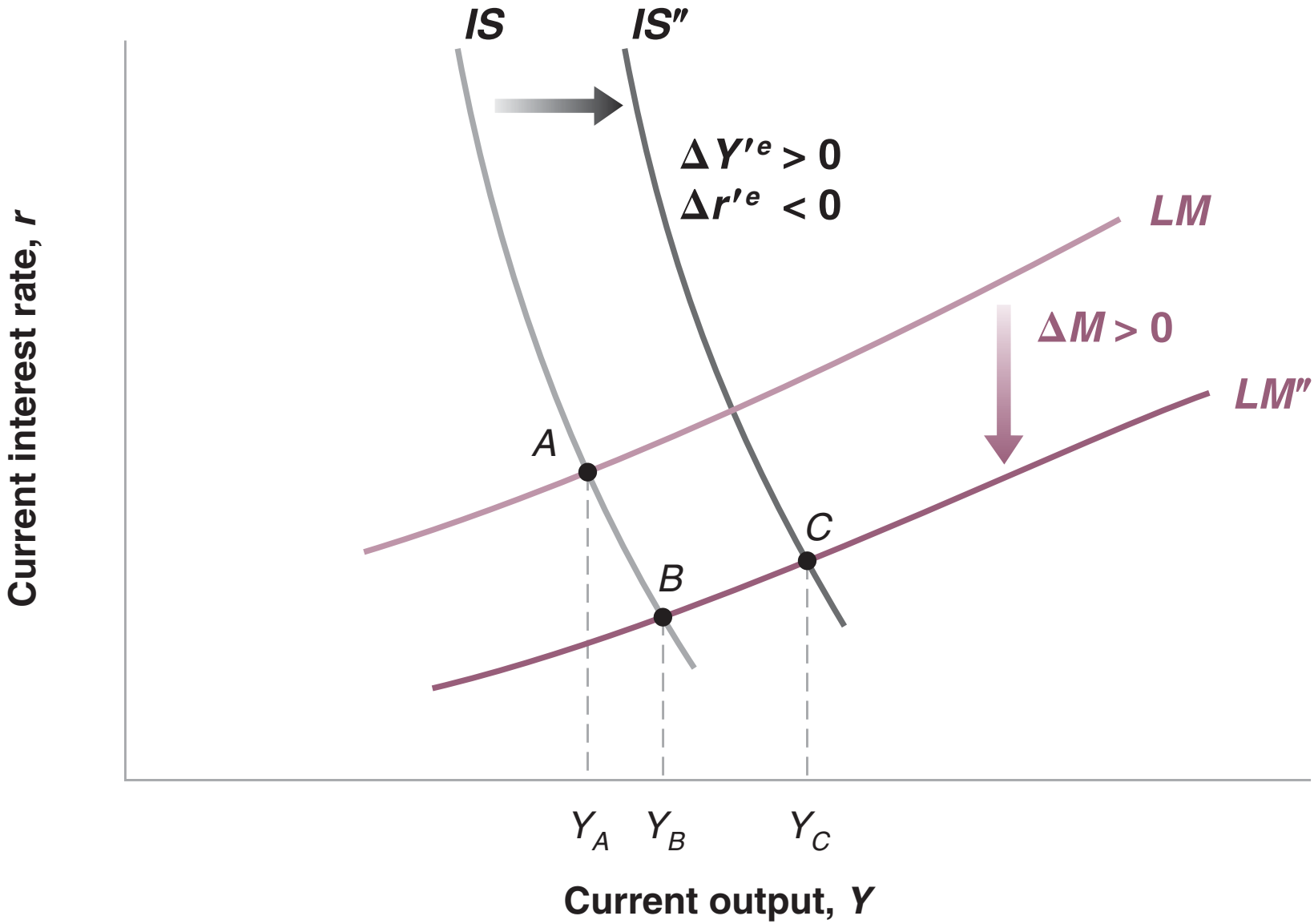
(future values)

Liquidity Trap



MT ↑

Expectations: Monetary Policy



Transitory $M\uparrow$: $A \to B$. Persistent $M\uparrow$: $A \to C$

Expectations: Monetary Policy

Key point

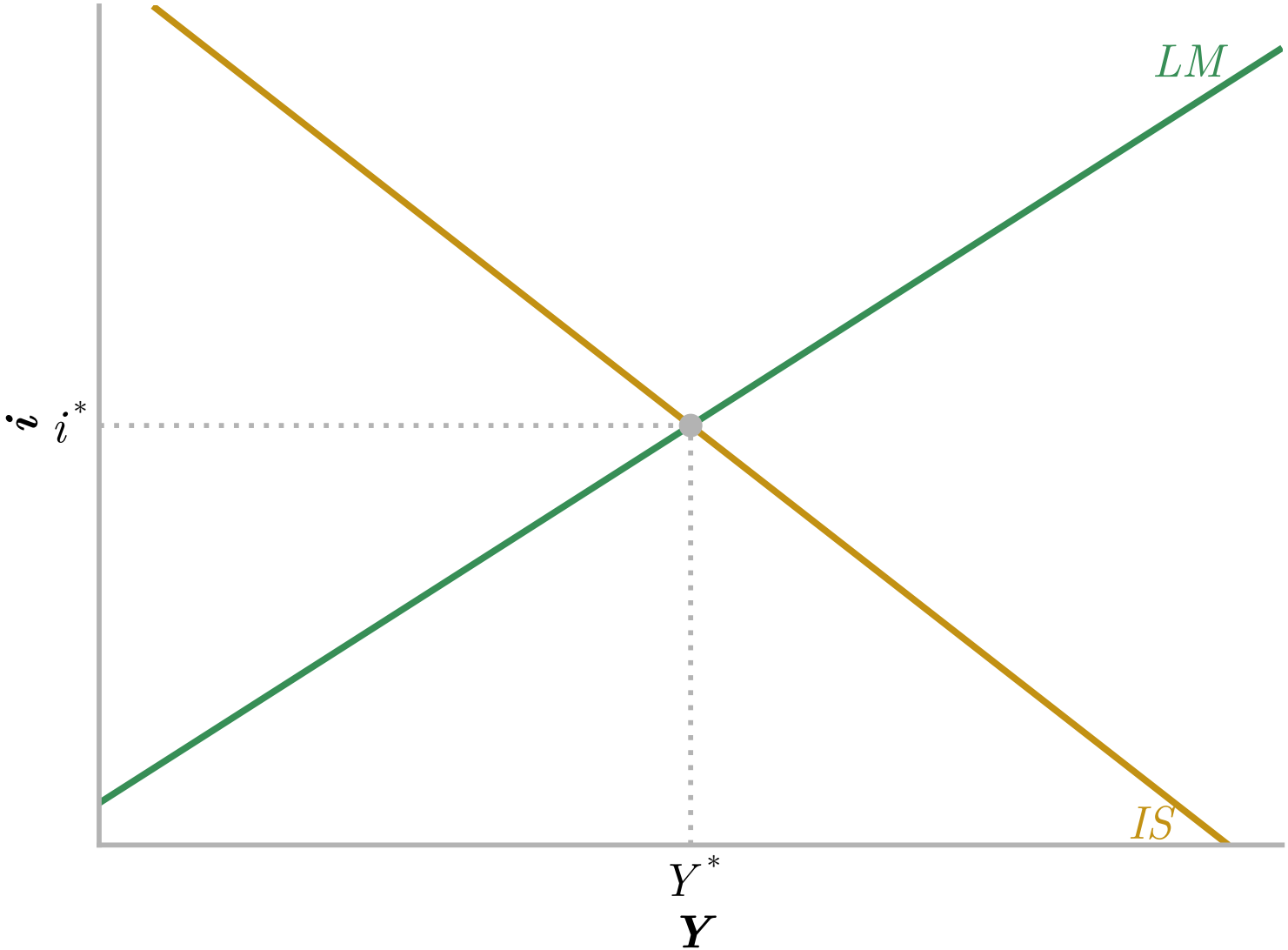
Monetary policy is more powerful, if it can change expectations.

Example

Quantitative Easing
The Fed buys large amounts of long-term bonds.
Signals that interest rates will remain low for a long time.

Expectations: Fiscal Policy

Can a cut in government spending stimulate aggregate demand?



A Few Major Caveats

The IS-LM model makes the government look too powerful.

- By raising G it can achieve any level of Y.
- When is this a reasonable shortcut?

Need spare capacity (no supply constraints)

It looks like saving lowers output.

- What is missing?

C↑ ⇒ S↓ ⇒ future capital stock ↓

Why Do We Still Have Recessions?

In the model, the government can stabilize output too easily.

Real world complications:

1. Big and variable lags until policies become effective
2. Lags in diagnosis and implementation of policies
3. Expansionary fiscal policies create debt
4. Expansionary monetary policies create inflation

An important point to remember

The IS-LM model makes strong assumptions: fixed prices, elastic supply, government can borrow without cost.
When applying the model, you need to consider how these assumptions modify the results.
(Or build a more comprehensive model)

Reading

Blanchard (2018), ch. 5 and 9.2; ch. 17 on expectations.

References I

Blanchard, O. (2018): *Macroeconomics*, Boston: Pearson, 8th ed.